



- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

# ALGORITHMIC METHODS FOR FORMAL VERIFICATION

by Yaniv Sa'ar

Supervisors: Prof. Amir Pnueli, Prof. Lenore D. Zuck, and  
Prof. David Harel

Department of Computer Science and Applied Mathematics  
Weizmann Institute of Science

July 10, 2011 / Ph.D. Defense

## Algorithmic Methods for Formal Verification

by Yaniv Sa'ar

### Introduction

### JTLV

### Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

### Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

### Misc. Developments

### Conclusion

## Thesis

A little software engineering in verification  
techniques goes a long way.

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

- Currently formal verification tools are black boxes
  - Hard to incorporate new model checking algorithms, unless one is familiar with tool (low-level C code)
- An exception is TLV (**Temporal Logic Verifier**)
  - TLV slightly changed the usual design perspective
  - Special purpose scripting language to create and manipulate BDDs on-the-fly
  - Tightly coupled with BDD package (CMU smv)

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

- Currently formal verification tools are black boxes
  - Hard to incorporate new model checking algorithms, unless one is familiar with tool (low-level C code)
- An exception is TLV (**Temporal Logic Verifier**)
  - TLV slightly changed the usual design perspective
  - **Special purpose** scripting language to create and manipulate BDDs on-the-fly
  - **Tightly coupled** with BDD package (CMU SMV)

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

- Currently formal verification tools are black boxes
  - Hard to incorporate new model checking algorithms, unless one is familiar with tool (low-level C code)
- An exception is TLV (**Temporal Logic Verifier**)
  - TLV slightly changed the usual design perspective
  - **Special purpose** scripting language to create and manipulate BDDs on-the-fly
  - **Tightly coupled** with BDD package (CMU SMV)

There is a need for easier-to-use developing environment!

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

There is a need for easier-to-use developing environment!

**JTLV** *Java Temporal Logic enVironment*:

- Computer-aided verification framework
- Allows for easy development of formal algorithms, in a high-level programming environment (e.g., verification, analysis, synthesis, abstraction)
- On top of state-of-the-art IDE; Eclipse
- Without having to sacrifice performance

## Algorithmic Methods for Formal Verification

by Yaniv Sa'ar

### Introduction

### JTLV

### Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

### Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

### Misc. Developments

### Conclusion

- 1 Introduction
- 2 A Framework for Developing Verification Algorithms
- 3 Synthesis
  - Synthesis of Reactive(1) Designs
  - AspectLTL: An Aspect Language for LTL Specifications
- 4 Compositional Methods
  - SPLIT: A Compositional LTL Verifier
  - Parallelizing A Symbolic Compositional Model-Checking Algorithm
  - A Dash of Fairness for Compositional Reasoning
- 5 Miscellaneous Developments
- 6 Conclusion

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

- Automatic synthesis of programs and (digital) designs from logical specifications is one of the most ambitious and challenging problems in computer science
- A solution would lift programming from the current mostly imperative level, to a declarative, logical style
- This is of major importance when concurrency is involved



- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

Synthesis process for general LTL has been identified as hopelessly intractable, yet:

- We identify an important and expressive fragment of LTL (GR(1)) which we can synthesize in quadratic time

# AspectLTL: An Aspect Language for LTL Specifications

Algorithmic Methods for  
Formal Verification

by Yaniv Sa'ar

Introduction

JTLV

Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

Misc. Developments

Conclusion

- Declarative language for specification and implementation of **crosscutting concerns**, based on LTL
- Supported by a JTLV-based prototype tool, that (literally) lifts declarative programming into practice
  - Generation of LTL aspect composition and synthesis is sound and complete
- Synthesis of GR(1) is an integral part of the compilation process

## Algorithmic Methods for Formal Verification

by Yaniv Sa'ar

### Introduction

### JTLV

### Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

### Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

### Misc. Developments

### Conclusion

- Model checking suffers from state explosion
- In the case of asynchronous concurrent systems, **local reasoning** can often ameliorate the problem

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

- Model checking suffers from state explosion
- In the case of asynchronous concurrent systems, **local reasoning** can often ameliorate the problem

Reachable  
States

Reachable  
States

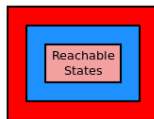
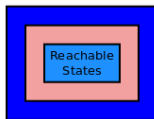
- Model checking suffers from state explosion
- In the case of asynchronous concurrent systems, **local reasoning** can often ameliorate the problem



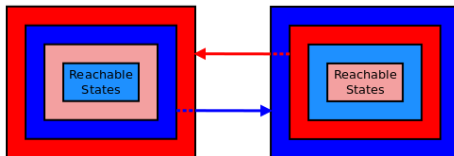
- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

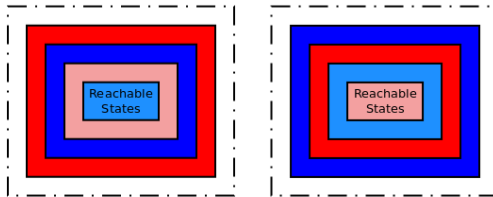
- Model checking suffers from state explosion
- In the case of asynchronous concurrent systems, **local reasoning** can often ameliorate the problem



- Model checking suffers from state explosion
- In the case of asynchronous concurrent systems, **local reasoning** can often ameliorate the problem

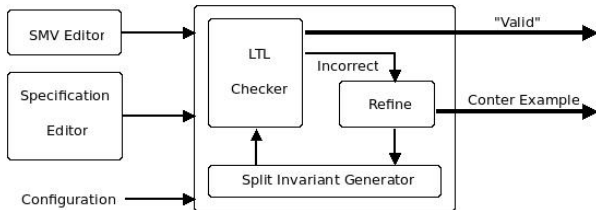


- Model checking suffers from state explosion
- In the case of asynchronous concurrent systems, **local reasoning** can often ameliorate the problem





- SPLIT is the first tool to implement a fully automated compositional method for arbitrary LTL properties



# Parallelizing A Symbolic Compositional Model-Checking Algorithm

Algorithmic Methods for  
Formal Verification

by Yaniv Sa'ar

Introduction

JTLV

Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

Misc. Developments

Conclusion

- Many attempts were made to parallelize model checking under general settings
- For compositional reasoning, both interference-freedom and locality suggest distributing each local computation.
  - How to distribute the computations?
  - How to handle the BDD structure(s)?
- Our solution:
  - BDD manager for each local computation
  - BDD communication between threads by copy
  - Number of threads slightly larger than number of cores
  - Good thread topology (usually star)

# A Dash of Fairness for Compositional Reasoning

Algorithmic Methods for  
Formal Verification

by Yaniv Sa'ar

Introduction

JTLV

Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

Misc. Developments

Conclusion

- Fairness is necessary for liveness
- Incorporating (global) fairness compositionally is difficult
- Previous work handles justice
- We developed a new algorithm to verify general LTL formulae for systems with compassion

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

## Two-Way Traceability and Conflict Debugging for AspectLTL

JTLV enables traceability and debugging support for AspectLTL programs.

## Verification of Multi-Linked Heaps

JTLV enables the automatic reasoning on programs that perform destructive updating on heaps.

## All You Need is Compassion

There are cases where mechanical solution is not good enough.

## Algorithmic Methods for Formal Verification

by Yaniv Sa'ar

### Introduction

### JTLV

### Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

### Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

### Misc. Developments

### Conclusion

## Thesis

A little software engineering in verification  
techniques goes a long way.

## Algorithmic Methods for Formal Verification

by Yaniv Sa'ar

### Introduction

### JTLV

### Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

### Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

### Misc. Developments

### Conclusion

- 1 Introduction
- 2 A Framework for Developing Verification Algorithms
- 3 Synthesis
  - Synthesis of Reactive(1) Designs
  - AspectLTL: An Aspect Language for LTL Specifications
- 4 Compositional Methods
  - SPLIT: A Compositional LTL Verifier
  - Parallelizing A Symbolic Compositional Model-Checking Algorithm
  - A Dash of Fairness for Compositional Reasoning
- 5 Miscellaneous Developments
- 6 Conclusion

Verification tools are based on two common elements.

- **Computational Model** – represents the system implementation
  - Representation for the various programming languages
  - Assigns a semantics to each reactive system
- **Specification Language** – represents the expectations from the implementation
  - Essentially temporal logic
  - The semantics of the computational structures serves as models for the formula

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

- Currently formal verification tools are black boxes
  - Hard to incorporate new model checking algorithms, unless one is familiar with tool (low-level C code)
- An exception is TLV (**Temporal Logic Verifier**)
  - TLV slightly changed the usual design perspective
  - **Special purpose** scripting language to create and manipulate BDDs on-the-fly
  - **Tightly coupled** with BDD package (CMU SMV)



- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

There is a need for easier-to-use developing environment!

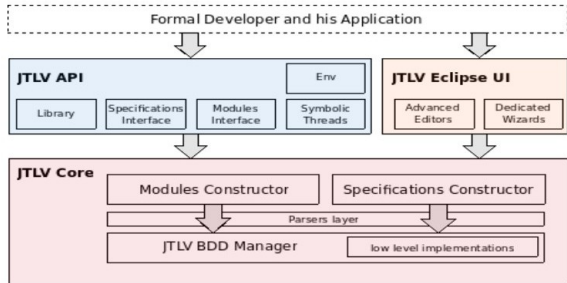
## JTLV *Java Temporal Logic enVironment*:

- Computer-aided verification framework
- Allows for easy development of formal algorithms, in a high-level programming environment (e.g., verification, analysis, synthesis, abstraction)
- On top of state-of-the-art IDE; Eclipse
- Without having to sacrifice performance

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

JTLV is composed of three major components:



## API:

- **Env** – Basic functionalities, e.g. load modules and specifications, save and load BDD to and from files, etc.
- **OpenVDL** – Open Verification Developer Library, contains implementations of known formal algorithms
- **Module** – A pure Java interface to the SMV code
- **Specification** – A pure Java interface to the specifications
- **Symbolic Threads** – Each instance is coupled with its own BDD manager, allowing it to execute freely without synchronization with other threads

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

So, . . . what can we do with it?

- **Advanced software engineering techniques:**
  - Object oriented design, and patterns
  - Increasing level of (programming) abstraction
  - Symbolic multi-threaded algorithms
- **Java/Eclipse ecosystem with respect to JTLV:**
  - Debugger, software verifiers, documentation methodology (JavaDoc), scripting environment (BeanShell), code refactoring, unit testing, etc.

# JTLV: A Framework for Developing Verification Algorithms

Algorithmic Methods for  
Formal Verification

by Yaniv Sa'ar

Introduction

JTLV

Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

Misc. Developments

Conclusion

So, . . . what can we do with it?

- Advanced software engineering techniques:
  - Object oriented design, and patterns
  - Increasing level of (programming) abstraction
  - Symbolic multi-threaded algorithms
- Java/Eclipse ecosystem with respect to JTLV:
  - Debugger, software verifiers, documentation methodology (JavaDoc), scripting environment (BeanShell), code refactoring, unit testing, etc.

So... what can we do with it?

- Advanced software engineering techniques:
  - Object oriented design, and patterns
  - Increasing level of (programming) abstraction
  - Symbolic multi-threaded algorithms
- Java/Eclipse ecosystem with respect to JTLV:
  - Debugger, software verifiers, documentation methodology (JavaDoc), scripting environment (BeanShell), code refactoring, unit testing, etc.

## Conclusion

JTLV makes symbolic techniques easier.  
(demonstrated in rest of talk)

## Algorithmic Methods for Formal Verification

by Yaniv Sa'ar

### Introduction

### JTLV

### Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

### Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

### Misc. Developments

### Conclusion

- Automatic synthesis of programs and (digital) designs from logical specifications is one of the most ambitious and challenging problems in computer science
- A solution would lift programming from the current mostly imperative level, to a declarative, logical style
- This is of major importance when concurrency is involved

# Synthesis of Reactive(1) Designs

Algorithmic Methods for  
Formal Verification

by Yaniv Sa'ar

Introduction

JTLV

Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

Misc. Developments

Conclusion

Synthesis process for general LTL has been identified as hopelessly intractable ([Pnueli, Rosner 89]), yet:



# Synthesis of Reactive(1) Designs

## Algorithmic Methods for Formal Verification

by Yaniv Sa'ar

### Introduction

### JTLV

### Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

### Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

### Misc. Developments

### Conclusion

Synthesis process for general LTL has been identified as hopelessly intractable ([Pnueli, Rosner 89]), yet:

- [Asarin, Maler, Pnueli, Sifakis 98]: (cubic) polynomial solutions to games (and synthesis) where the acceptance condition is:  $\Box p$ ,  $\Diamond q$ ,  $\Box \Diamond p$ , or  $\Diamond \Box q$
- [Alur, La Torre 04]: efficient synthesis for Boolean combinations of formulae of the form  $\Box p$

Synthesis process for general LTL has been identified as hopelessly intractable ([Pnueli, Rosner 89]), yet:

- We present a quadratic game-based synthesis algorithm for **General Reactivity of rank 1** (GR(1)) specifications:

$$(\Box \Diamond p_1 \wedge \cdots \wedge \Box \Diamond p_m) \rightarrow (\Box \Diamond q_1 \wedge \cdots \wedge \Box \Diamond q_n)$$

where each  $p_i$  and  $q_i$  is a Boolean combination of atomic propositions

## GR(1) fragment

$$(\Box \Diamond p_1 \wedge \cdots \wedge \Box \Diamond p_m) \rightarrow (\Box \Diamond q_1 \wedge \cdots \wedge \Box \Diamond q_n)$$

- Specifications are usually exponentially more succinct than their implementations
- Past LTL formulae can be included in both assumptions and guarantees

## GR(1) fragment

$$(\Box \Diamond p_1 \wedge \cdots \wedge \Box \Diamond p_m) \rightarrow (\Box \Diamond q_1 \wedge \cdots \wedge \Box \Diamond q_n)$$

- GR(1) seems to place an undue burden on the user or have a too restrictive expressive power
  - Assume/Guarantee specifications are common practice in industry
  - Expressiveness of GR(1) is well established
  - Solution to GR(1) implies a solution to GR(k) ( $\bigwedge_k$  GR(1)) that is exponential in  $k$ . GR(k) is at the top of LTL hierarchy

# Synthesis of Reactive(1) Designs

Algorithmic Methods for  
Formal Verification

by Yaniv Sa'ar

Introduction

JTLV

Synthesis

– Synthesis of Reactive(1) Designs

– AspectLTL: An Aspect Language for  
LTL Specifications

Compositional Methods

– SPLIT: A Compositional LTL Verifier

– Parallelizing A Symbolic  
Compositional Model-Checking

– A Dash of Fairness for  
Compositional Reasoning

Misc. Developments

Conclusion

GR(1) fragment

$$\underbrace{(\Box \Diamond p_1 \wedge \cdots \wedge \Box \Diamond p_m)}_{\text{Assume}} \rightarrow \underbrace{(\Box \Diamond q_1 \wedge \cdots \wedge \Box \Diamond q_n)}_{\text{Guarantee}}$$

- GR(1) seems to place an undue burden on the user or have a too restrictive expressive power
  - Assume/Guarantee specifications are common practice in industry
  - Expressiveness of GR(1) is well established
  - Solution to GR(1) implies a solution to GR(k) ( $\bigwedge_k \text{GR}(1)$ ) that is exponential in  $k$ . GR(k) is at the top of LTL hierarchy

## GR(1) fragment

$$\underbrace{(\Box \Diamond p_1 \wedge \cdots \wedge \Box \Diamond p_m)}_{\text{Assume}} \rightarrow \underbrace{(\Box \Diamond q_1 \wedge \cdots \wedge \Box \Diamond q_n)}_{\text{Guarantee}}$$

- GR(1) seems to place an undue burden on the user or have a too restrictive expressive power
  - Assume/Guarantee specifications are common practice in industry
  - Expressiveness of GR(1) is well established
  - Solution to GR(1) implies a solution to GR(k) ( $\bigwedge_k$  GR(1)) that is exponential in  $k$ . GR(k) is at the top of LTL hierarchy

# Synthesis of Reactive(1) Designs

Algorithmic Methods for  
Formal Verification

by Yaniv Sa'ar

Introduction

JTLV

Synthesis

– Synthesis of Reactive(1) Designs

– AspectLTL: An Aspect Language for  
LTL Specifications

Compositional Methods

– SPLIT: A Compositional LTL Verifier

– Parallelizing A Symbolic  
Compositional Model-Checking

– A Dash of Fairness for  
Compositional Reasoning

Misc. Developments

Conclusion

GR(1) fragment

$$\underbrace{(\Box \Diamond p_1 \wedge \cdots \wedge \Box \Diamond p_m)}_{\text{Assume}} \rightarrow \underbrace{(\Box \Diamond q_1 \wedge \cdots \wedge \Box \Diamond q_n)}_{\text{Guarantee}}$$

- GR(1) seems to place an undue burden on the user or have a too restrictive expressive power
  - Assume/Guarantee specifications are common practice in industry
  - Expressiveness of GR(1) is well established
  - Solution to GR(1) implies a solution to GR(k) ( $\bigwedge_k \text{GR}(1)$ ) that is exponential in  $k$ . GR(k) is at the top of LTL hierarchy

## Algorithmic Methods for Formal Verification

by Yaniv Sa'ar

### Introduction

### JTLV

### Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

### Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

### Misc. Developments

### Conclusion

- The synthesis heavily uses symbolic analysis of state space
- The synthesis, with all its stages, was implemented in JTLV



# Synthesis of Reactive(1) Designs

## Algorithmic Methods for Formal Verification

by Yaniv Sa'ar

### Introduction

### JTLV

### Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

### Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

### Misc. Developments

### Conclusion

- The synthesis heavily uses symbolic analysis of state space
- The synthesis, with all its stages, was implemented in JTLV

## Conclusion

The high complexity established for LTL synthesis does not necessarily identify it as intractable. JTLV allows for efficient mechanization of the synthesis.

# AspectLTL: An Aspect Language for LTL Specifications

Algorithmic Methods for  
Formal Verification

by Yaniv Sa'ar

Introduction

JTLV

Synthesis

– Synthesis of Reactive(1) Designs

– AspectLTL: An Aspect Language for  
LTL Specifications

Compositional Methods

– SPLIT: A Compositional LTL Verifier

– Parallelizing A Symbolic  
Compositional Model-Checking

– A Dash of Fairness for  
Compositional Reasoning

Misc. Developments

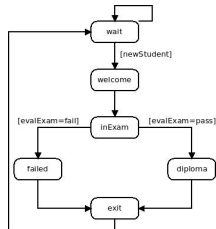
Conclusion

- Declarative language for specification and implementation of **crosscutting concerns**, based on LTL
- Supported by a JTLV-based prototype tool, that (literally) lifts declarative programming into practice
  - Generation of LTL aspect composition and synthesis is sound and complete
- Synthesis of GR(1) is an integral part of the compilation process

## Exam service

```

MODULE ExamService
VARENV -- environment variables
  evalExam : {pass, fail};
  newStudent : boolean;
VAR -- system variables
  state : {wait, welcome, inExam, diploma,
          failed, exit};
INIT
  state=wait;
TRANS
  ((state=wait) -> ( (next(state)=wait) |
                    (newStudent & next(state)=welcome) )) &
  ((state=welcome) -> (next(state)=inExam) &
  (state=inExam)
  -> ( (next(state)=diploma &
        next(evalExam)=pass ) |
        (next(state)=failed &
        next(evalExam)=fail) ) ) &
  ((state=diploma) -> (next(state)=exit)) &
  ((state=failed) -> (next(state)=exit)) &
  ((state=exit) -> (next(state)=wait));
  
```





# AspectLTL: An Aspect Language for LTL Specifications

Algorithmic Methods for Formal Verification

by Yaniv Sa'ar

Introduction

JTLV

Synthesis

- Synthesis of Reactive(1) Designs

- AspectLTL: An Aspect Language for LTL Specifications

Compositional Methods

- SPLIT: A Compositional LTL Verifier

- Parallelizing A Symbolic Compositional Model-Checking

- A Dash of Fairness for Compositional Reasoning

Misc. Developments

Conclusion

## Exam service – with a tuition concern

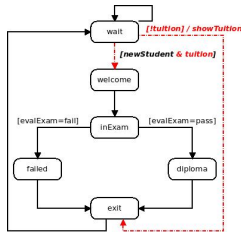
```

MODULE ExamService
VARENV -- environment variables
  evalExam : {pass, fail};
  newStudent : boolean;
VAR -- system variables
  state : {wait, welcome, inExam, diploma,
          failed, exit};
INIT
  state=wait;
TRANS
  ((state=wait) -> ( (next(state)=wait) |
                    (newStudent & next(state)=welcome) )) &
  ((state=welcome) -> (next(state)=inExam) &
  (state=inExam)
  -> ( (next(state)=diploma &
        next(evalExam)=pass ) |
        (next(state)=failed &
        next(evalExam)=fail) ) ) &
  ((state=diploma) -> (next(state)=exit)) &
  ((state=failed) -> (next(state)=exit)) &
  ((state=exit) -> (next(state)=wait));
  
```

+

```

ASPECT Tuition
VARENV -- environment variables
  new tuition : boolean;
VAR -- system variables
  ext state : {wait, welcome, exit};
  new showTuition : boolean;
TRANS
  -- adding a transition from wait directly
  -- to exit if the tuition was not paid.
  ( state=wait & next(state)=exit &
    !tuition & next(showTuition) );
LTLSPEC
  -- there is no transition from wait to
  -- welcome if the tuition was not paid.
  [] (!(state=wait & !tuition &
        next(state)=welcome) );
  
```



- AspectLTL supports the language features considered as distinguishing characteristics of aspect languages:
  - **Obliviousness** – the base system makes no assumptions about LTL aspects
  - **Quantification** – an aspects assumes little about the base system (allowing modularity of concerns)

# AspectLTL: An Aspect Language for LTL Specifications

## Algorithmic Methods for Formal Verification

by Yaniv Sa'ar

## Introduction

## JTLV

## Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

## Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

## Misc. Developments

## Conclusion

- As opposed to prior works, ours addresses the correct composition at the **semantics** level
- We use GR(1) to define a novel **declarative style** programming language
- The language is supported by a JTLV-based prototype

# AspectLTL: An Aspect Language for LTL Specifications

Algorithmic Methods for  
Formal Verification

by Yaniv Sa'ar

Introduction

JTLV

Synthesis

– Synthesis of Reactive(1) Designs

AspectLTL: An Aspect Language for  
LTL Specifications

Compositional Methods

– SPLIT: A Compositional LTL Verifier

– Parallelizing A Symbolic  
Compositional Model-Checking

– A Dash of Fairness for  
Compositional Reasoning

Misc. Developments

Conclusion

- As opposed to prior works, ours addresses the correct composition at the **semantics** level
- We use GR(1) to define a novel **declarative style** programming language
- The language is supported by a JTLV-based prototype

## Conclusion

AspectLTL lifts programming from the current, mostly imperative style, to a declarative, logical style. JTLV enables the development of an efficient compiler for the language.

- Model checking suffers from state explosion
- In the case of asynchronous concurrent systems, **local reasoning** can often ameliorate the problem
- [Namjoshi 05] Construct a vector, **split invariant**, of local (i.e., per-process) inductive invariants,

$$\theta = \theta_1, \theta_2, \dots, \theta_n$$

- **interference-free** – a step by one process does not violate the invariant of another
- the conjunction of local invariants ( $\bigwedge_i \theta_i$ ), is always **globally inductive invariant**
- **Locality** is enforced syntactically



- Model checking suffers from state explosion
- In the case of asynchronous concurrent systems, **local reasoning** can often ameliorate the problem
- [Namjoshi 05] Construct a vector, **split invariant**, of local (i.e., per-process) inductive invariants,

$$\theta = \theta_1, \theta_2, \dots, \theta_n$$

- **interference-free** – a step by one process does not violate the invariant of another
- the conjunction of local invariants ( $\bigwedge_i \theta_i$ ), is always **globally inductive** invariant
- **Locality** is enforced syntactically

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

## Split invariant computation:

Reachable  
States

Reachable  
States

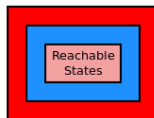
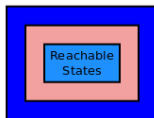
- Reachability analysis: PSPACE(N)-complete.  
Computation of split invariant: PTIME(N) and incomplete
- [Cohen, Namjoshi 07] automatically refine using *auxiliary variables* yielding completeness

## Split invariant computation:



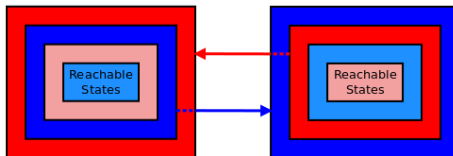
- Reachability analysis: PSPACE(N)-complete.  
Computation of split invariant: PTIME(N) and incomplete
- [Cohen, Namjoshi 07] automatically refine using *auxiliary variables* yielding completeness

## Split invariant computation:



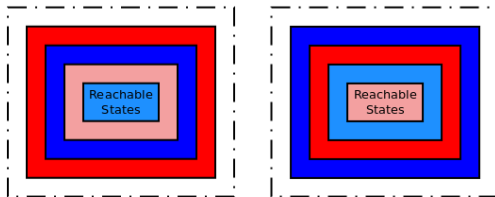
- Reachability analysis: PSPACE(N)-complete. Computation of split invariant: PTIME(N) and incomplete
- [Cohen, Namjoshi 07] automatically refine using *auxiliary variables* yielding completeness

## Split invariant computation:



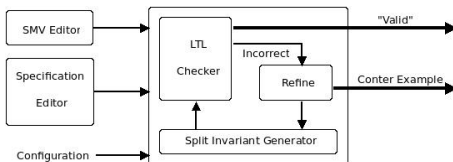
- Reachability analysis: PSPACE(N)-complete. Computation of split invariant: PTIME(N) and incomplete
- [Cohen, Namjoshi 07] automatically refine using *auxiliary variables* yielding completeness

## Split invariant computation:



- Reachability analysis: PSPACE(N)-complete. Computation of split invariant: PTIME(N) and incomplete
- [Cohen, Namjoshi 07] automatically refine using *auxiliary variables* yielding completeness

- SPLIT is an overarching system implementing:
  1. Simultaneous least fixpoint [Namjoshi 05]
  2. [Cohen, Namjoshi 07] safety refinement (completeness)
  3. [Cohen, Namjoshi 08] algorithm for progress under justice
  4. [CNS10a] algorithm for arbitrary LTL properties under both justice and compassion



- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

- Experimental results support claim that local reasoning allows verifying *significantly* larger systems
- SPLIT is the first tool to implement a fully automated compositional method for arbitrary LTL properties

## Conclusion

JTLV enabled the development of a complete off-the-shelf standalone application for fully compositional reasoning.



# Parallelizing A Symbolic Compositional Model-Checking Algorithm

Algorithmic Methods for  
Formal Verification

by Yaniv Sa'ar

Introduction

JTLV

Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking

- A Dash of Fairness for Compositional Reasoning

Misc. Developments

Conclusion

- Many attempts were made to parallelize model checking under general settings
- For compositional reasoning, both interference-freedom and locality suggest distributing each local computation.
  - How to distribute the computations?
  - How to handle the BDD structure(s)?
- Our solution:
  - BDD manager for each local computation
  - BDD communication between threads by copy
  - Number of threads slightly larger than number of cores
  - Good thread topology (usually star)

# Parallelizing A Symbolic Compositional Model-Checking Algorithm

Algorithmic Methods for Formal Verification

by Yaniv Sa'ar

Introduction

JTLV

Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking

- A Dash of Fairness for Compositional Reasoning

Misc. Developments

Conclusion

N	sequential	4 cores			8 cores		
	Time	Time	Speedup	Eff.	Time	Speedup	Eff.
MUX-SEM							
512	27	8.3	3.25	0.81	4.8	5.6	0.70
1024	117	34.8	3.3	0.82	19.2	6.1	0.76
1536	360	112	3.2	0.80	65	5.5	0.69
2048	561	165	3.4	0.85	92	6.1	0.76
SZYMANSKI							
5	3.1	1.6	1.93	0.48	1.1	2.81	0.35
6	20.5	6.5	3.15	0.78	4.4	4.65	0.78
7	130	41	3.17	0.79	23.7	5.48	0.78
8	564	163	3.46	0.86	93	6.06	0.76
9	2896	739	3.91	0.97	492	5.88	0.73
GERMAN							
9	489	126	3.88	0.97	76	6.40	0.80
10	1076	268	4.00	1.00	164	6.56	0.82
11	2867	691	4.14	1.03	385	7.44	0.93
12	over BDD limit	1819	-	-	1013	-	-
PETERSON'S							
4	0.7	0.9	0.77	0.19	0.9	0.77	0.17
5	8.5	4	2.1	0.50	3.2	2.6	0.52
6	183	66	2.77	0.70	46	3.98	0.66

# Parallelizing A Symbolic Compositional Model-Checking Algorithm

Algorithmic Methods for  
Formal Verification

by Yaniv Sa'ar

Introduction

JTLV

Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

Misc. Developments

Conclusion

- Multi-core processing is a promising direction for next generation model checking
- Compositional algorithms can exploit the multi-core
- JTLV is an ideal environment to develop multi-processing applications

## Conclusion

Model checking on multi-core architectures is a promising direction. JTLV enables the development non-trivial multi-threaded applications.

# A Dash of Fairness for Compositional Reasoning

## Algorithmic Methods for Formal Verification

by Yaniv Sa'ar

### Introduction

### JTLV

### Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

### Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

### Misc. Developments

### Conclusion

- Fairness is necessary for liveness
- Incorporating (global) fairness compositionally is difficult
- Previous work handles justice
- We developed a new algorithm to verify general LTL formulae for systems with compassion

1. Compute the split invariant vector  $\langle \theta_1, \theta_2, \dots, \theta_n \rangle$
2. For each process  $P_i$  build an abstraction  $Q_i$  containing transitions  $T_i$ , and **summaries** of others transitions
  - Summary  $S_j$  for  $P_j$  is defined as  $(\exists L_j, L'_j : \theta_j \wedge T_j)$
3. For each process  $P_i$  abstract others fairness conditions
  - A compassion  $\langle p_j, q_j \rangle$  of  $P_j$  is transformed to its corresponding abstraction
 
$$\langle \underbrace{\forall L_j : \theta_j \rightarrow p_j}_{\text{increasing states}}, \underbrace{\exists L_j : \theta_j \wedge q_j}_{\text{reducing states}} \rangle$$
4. Verify the property over every abstract process  $Q_i$
5. If the check succeeds, HALT with **success**
6. If all summary transitions in cex are concrete, HALT with **failure**. Otherwise, refine and RETURN to step 1

# A Dash of Fairness for Compositional Reasoning

## Algorithmic Methods for Formal Verification

by Yaniv Sa'ar

### Introduction

### JTLV

### Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

### Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

### Misc. Developments

### Conclusion

- New algorithm demonstrates how to handle compassion in compositional framework
- Experimental results are encouraging
- JTLV ideal for experiments

## Conclusion

Compositional reasoning can also handle compassion.  
JTLV makes reasoning simple.

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

## Two-Way Traceability and Conflict Debugging for AspectLTL

JTLV enables traceability and debugging support for AspectLTL programs.

## Verification of Multi-Linked Heaps

JTLV enables the automatic reasoning on programs that perform destructive updating on heaps.

## All You Need is Compassion

There are cases where mechanical solution is not good enough.

## Algorithmic Methods for Formal Verification

by Yaniv Sa'ar

### Introduction

### JTLV

### Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

### Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

### Misc. Developments

### Conclusion

There is a need for easier-to-use developing environment!

[PSZ10b]

JTLV makes symbolic techniques easier.



- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

There is a need for easier-to-use developing environment!

[PSZ10b]

JTLV makes symbolic techniques easier.

[PPS06, BPPS11]

The high complexity established for LTL synthesis does not necessarily identify it as intractable. JTLV allows for efficient mechanization of the synthesis.

[MS11]

AspectLTL lifts programming from the current, mostly imperative style, to a declarative, logical style. JTLV enables the development of an efficient compiler for the language.

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

There is a need for easier-to-use developing environment!

[PSZ10b]

JTLV makes symbolic techniques easier.

[CNS+10c]

Model checking on multi-core architectures is a promising direction. JTLV enables the development non-trivial multi-threaded applications.

[CNS10a]

Compositional reasoning can also handle compassion. JTLV makes reasoning simple.

[CNS10b]

JTLV enabled the development of a complete off-the-shelf standalone application for fully compositional reasoning.

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

There is a need for easier-to-use developing environment!

[PSZ10b]

JTLV makes symbolic techniques easier.

[MS12]

JTLV enables traceability and debugging support for AspectLTL programs.

[BPSZ11]

JTLV enables the automatic reasoning on programs that perform destructive updating on heaps.

[PS08]

There are cases where mechanical solution is not good enough.

## Algorithmic Methods for Formal Verification

by Yaniv Sa'ar

### Introduction

### JTLV

### Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

### Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

### Misc. Developments

### Conclusion

There is a need for easier-to-use developing environment!

[PSZ10b]

JTLV makes symbolic techniques easier.

### Other Users

We should also note that JTLV already has an avid user community, including researchers from Imperial College London, New York University, Bell Labs Alcatel-Lucent, Weizmann Institute, Microsoft Research Cambridge, RWTH-Aachen, California Institute of Technology, GRASP Laboratory University of Pennsylvania, and University of California Los Angeles.



- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

# ALGORITHMIC METHODS FOR FORMAL VERIFICATION

by Yaniv Sa'ar

Supervisors: Prof. Amir Pnueli, Prof. Lenore D. Zuck, and  
Prof. David Harel

Department of Computer Science and Applied Mathematics  
Weizmann Institute of Science

July 10, 2011 / Ph.D. Defense

# Partial Bibliography

## Algorithmic Methods for Formal Verification

by Yaniv Sa'ar

### Introduction

### JTLV

### Synthesis

- Synthesis of Reactive(1) Designs
- AspectLTL: An Aspect Language for LTL Specifications

### Compositional Methods

- SPLIT: A Compositional LTL Verifier
- Parallelizing A Symbolic Compositional Model-Checking
- A Dash of Fairness for Compositional Reasoning

### Misc. Developments

### Conclusion

- ▶ Amir Pnueli, Yaniv Sa'ar, and Lenore D. Zuck. *JTLV: A Framework for Developing Verification Algorithms*. In *Proc. 22nd Int. Conf. on Computer Aided Verification*, 2010.
- ▶ Nir Piterman, Amir Pnueli, and Yaniv Sa'ar. *Synthesis of Reactive(1) Designs*. In *Proc. 7th Int. Conf. on Verification, Model Checking, and Abstract Interpretation*, 2006.
- ▶ Roderick Bloem, Barbara Jobstmann, Nir Piterman, Amir Pnueli, and Yaniv Sa'ar. *Synthesis of Reactive(1) Designs*. *JCSS, Special Issue in Honor of Amir Pnueli*.
- ▶ Shahar Maoz and Yaniv Sa'ar. *AspectLTL: An Aspect Language for LTL Specifications*. In *Proc. 10th Int. Conf. on Aspect-Oriented Software Development*, 2011..
- ▶ Ariel Cohen, Kedar S. Namjoshi, Yaniv Sa'ar, Lenore D. Zuck, and Katya I. Kisyova. *Parallelizing a Symbolic Compositional Model-Checking Algorithm*. In *Proc. 6th Int. Haifa Verification Conf.*, 2010.
- ▶ Ariel Cohen, Kedar S. Namjoshi, and Yaniv Sa'ar. *A Dash of Fairness for Compositional Reasoning*. In *Proc. 22nd Int. Conf. on Computer Aided Verification*, 2010.
- ▶ Ariel Cohen, Kedar S. Namjoshi, and Yaniv Sa'ar. *SPLIT: A Compositional LTL Verifier*. In *Proc. 22nd Int. Conf. on Computer Aided Verification*, 2010.
- ▶ Ittai Balaban, Amir Pnueli, Yaniv Sa'ar, and Lenore D. Zuck. *Verification of Multi-Linked Heaps*. *JCSS, Special Issue in Honor of Amir Pnueli*.
- ▶ Shahar Maoz and Yaniv Sa'ar. *Two-way Traceability and Conflict Debugging for AspectLTL Programs*. In *Proc. 11th Int. Conf. on Aspect-Oriented Software Development*, 2012. Submitted.
- ▶ Amir Pnueli and Yaniv Sa'ar. *All You Need is Compassion*. In *Proc. 9th Int. Conf. on Verification, Model Checking, and Abstract Interpretation*, 2008.